# The Crystal Structure of the High Pressure Phase, $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$, and Polymorphism in $\mathrm{CaB}_{2} \mathrm{O}_{4}$ 

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#### Abstract

$\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$ is a high pressure phase of calcium metaborate. Single crystals were grown at 30 kbar and $900^{\circ} \mathrm{C}$. They were found to be cubic with $a=9.008 \pm 0.001 \AA, Z=12, d_{c}=3.426 \mathrm{~g} . \mathrm{cm}^{-3}$ and space group symmetry Pa3.

The structure has been determined by a three-dimensional Fourier synthesis. The positional and isotropic thermal parameters have been refined by the least-squares method based on 267 structure factors. The final conventional $R$ value is 0.033 . All the boron atoms are tetrahedrally coordinated. The mean B-O distance is $1.480 \AA$. There are two independent Ca atoms. $\mathrm{Ca}(1)$ is surrounded by a 12 -oxygen polyhedron with two sets of Ca-O distances of $2.671 \AA$ and $2.785 \AA$. This is the first observation of coordination twelve for calcium. $\mathrm{Ca}(2)$ is also surrounded by twelve oxygens, but the polyhedron formed by these oxygen atoms is very irregular. There are four sets of $\mathrm{Ca}-\mathrm{O}$ distances: 2.385, $2 \cdot 483,2 \cdot 598$ and $3 \cdot 142 \AA$. The coordination number of the oxygen atoms is five; each one is surrounded by one $\mathrm{Ca}(1)$, two $\mathrm{Ca}(2)$, and two boron atoms.

Calcium metaborate can crystallize with four different structures by varying the pressure at which the synthesis is carried out. The common trend among these structures is an increase of the cation coordination with increasing pressure. By analogy many new phases of borates and polyborates could be synthesized under pressure.


## Introduction

Calcium metaborate can be prepared in four crystalline modifications by varying the pressure at which the synthesis is carried out. A detailed structure study has been reported for $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})$ (Marezio, Plettinger \& Zachariasen, 1963b) and $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (III) (Marezio, Remeika \& Dernier, 1969). The precise crystal structure of $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{II})$ has been determined by Zachariasen (1968). This paper reports in detail the crystal-growth and the crystal structure determination of $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$. In addition, a discussion of the polymorphism of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ is given.

## Crystal growth

The starting material for all high pressure runs was $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})$. The procedure of the high pressure experiments was the same as has been described in the preceding paper.

The high pressure phase $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$ was first prepared in polycrystalline form by direct application of temperature and pressure to $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})$. A temperature of $900^{\circ} \mathrm{C}$ and a pressure of 30 kbar for one hour was sufficient to produce the desired phase change. It should be noted that each time $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$ was formed during the raising of the temperature, a pressure drop of 1 kbar was observed between $450^{\circ}$ and $500^{\circ} \mathrm{C}$. After quenching to room temperature and pressure, X-ray powder photographs of the quenched material showed that a fourth phase of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ had been retained metastably. The powder pattern of the new phase

[^0]could be indexed on a cubic cell of about $9 \AA$. Also, the new phase could be reconverted to the low pressure phase by annealing overnight at $750^{\circ} \mathrm{C}$ in air. The powder photographs of the annealed $\mathrm{CaB}_{2} \mathrm{O}_{4}$ and of the starting material were identical.

In order to obtain single crystals of $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$, powdered $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})$ was packed into a platinum cup of dimensions 2.6 mm internal diameter by 5.5 mm high, to which $20 \mu$ l of distilled water were added as a solvent. After one hour at 30 kbar and $900^{\circ} \mathrm{C}$, the sample was allowed to cool to room temperature at a rate of $30 \% \mathrm{~min}$. Then the pressure was released at a rate of approximately $2 \mathrm{kbar} / \mathrm{min}$. The platinum cell was broken open and many transparent crystals were found. A few large ( $\sim 1.5 \mathrm{~mm}$ long) crystals had a didodecahedral form but most crystals were fractured and of rather poor morphology. X-ray powder photographs of these crystals were identical to those of the polycrystalline $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$.

Optical analysis confirmed that the crystals of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (IV) are cubic. In addition to these isotropic crystals, in each run some very small, birefringent crystals were present. X-ray powder photographs showed that these crystals were $\mathrm{Ca}_{3}\left(\mathrm{BO}_{3}\right)_{2}$, meaning that a decomposition had taken place under pressure: $3 \mathrm{CaB}_{2} \mathrm{O}_{4} \rightarrow \mathrm{Ca}_{3}\left(\mathrm{BO}_{3}\right)_{2}+2 \mathrm{~B}_{2} \mathrm{O}_{3}$. More of this decomposition product was obtained at 40 kbar and $1000^{\circ} \mathrm{C}$ with $10 \mu l$ of distilled water as solvent. Furthermore, in the runs where a larger amount of water was used, needle-like crystals of a third phase were present. Subsequent high pressure experiments revealed that the yield of the needle-like crystals depended on the amount of water present. Most important was the fact that no reflections belonging to the needle-like phase
were detected in any of the X-ray powder photographs of the polycrystalline $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$ material. These observations seem to indicate that the needle-like crystals are a hydrate of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ or some product of decomposition of $\mathrm{CaB}_{2} \mathrm{O}_{4}$.

## Crystal data

The crystals of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (IV) were found to be cubic with $a=9.008 \pm 0.001 \AA$ and 12 molecules per unit cell. The calculated density is $3.426 \mathrm{~g} . \mathrm{cm}^{-3}$. The symmetry and the lattice parameter were determined from a powder film taken at room temperature with a Norelco camera of 114.6 cm in diameter and $\mathrm{Cr} K \alpha$ radiation. The lattice parameter was calculated by the leastsquares refinement program of Mueller, Heaton \& Miller (1960). A comparison of observed and calculated interplanar spacings and observed intensities is given in Table 1.

Table 1. Powder pattern of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (IV)

| $h^{2}+k^{2}+l^{2}$ | $d_{\text {obs }}$ | $d_{\text {cal }}$ | $I$ |
| :---: | :---: | :---: | :---: |
| 5 | $4 \cdot 008$ | 4.029 | $\boldsymbol{w}$ |
| 8 | $3 \cdot 172$ | 3.185 | $w$ |
| 9 | $2 \cdot 907$ | 3.003 | $w$ |
| 11 | $2 \cdot 708$ | 2.716 | $s$ |
| 13 | 2.489 | 2.498 | $m$ |
| 14 | $2 \cdot 402$ | $2 \cdot 407$ | $w m$ |
| 16 | $2 \cdot 246$ | 2.252 | $\boldsymbol{w}$ |
| 17 | 2.180 | 2.185 | wm |
| 18 | $2 \cdot 120$ | $2 \cdot 123$ | $\boldsymbol{w}$ |
| 19 | 2.065 | 2.067 | $v w$ |
| 20 | 2.011 | 2.014 | $m s$ |
| 21 | 1.962 | 1.966 | $s$ |
| 22 | 1.918 | 1.921 | $m s$ |
| 24 | 1.837 | 1.839 | $v w$ |
| 27 | 1.731 | 1.734 | wm |
| 29 | 1.669 | 1.673 | $\boldsymbol{w}$ |
| 30 | 1.641 | 1.645 | wm |
| 32 | $1 \cdot 590$ | 1.592 | wm |
| 33 | $1 \cdot 567$ | 1.568 | $v v w$ |
| 34 | $1 \cdot 544$ | 1.545 | $v w$ |
| 35 | $1 \cdot 519$ | 1.523 | $v w$ |
| 36 | 1.499 | 1.501 | $w$ |
| 38 | 1.459 | 1.461 | $m$ |
| 43 | 1.373 | 1.374 | $\boldsymbol{w}$ |
| 44 | $1 \cdot 357$ | 1.358 | $\boldsymbol{w}$ |
| 45 | $1 \cdot 342$ | $1 \cdot 343$ | $\boldsymbol{w}$ |
| 48 | 1.296 | 1.300 | $m$ |
| 53 | 1-237 | 1.237 | $m$ |
| 54 | $1 \cdot 225$ | 1.226 | $\boldsymbol{w}$ |
| 56 | 1.203 | 1.204 | $m s$ |
| 57 | $1 \cdot 193$ | 1.193 | $\boldsymbol{w}$ |
| 59 | $1 \cdot 173$ | $1 \cdot 173$ | $s$ |
| 61 | $1 \cdot 153$ | $1 \cdot 153$ | $\boldsymbol{w}$ |

Precession photographs taken with Mo $K \alpha$ showed that the systematic absences are: $k=2 n+1$ for $0 k l$, $l=2 n+1$ for $h 0 l$ and $h=2 n+1$ for $h k 0(h, k, l$ are not permutable). These absences lead to space group symmetry Pa3. Of the 12 calcium atoms, 4 are in the special positions $4(a)$ and 8 in the special positions $8(c)$. The boron atoms and the $O(1)$ and $O(2)$ atoms are in the general positions 24(d) (International Tables for $X$-ray Crystallography, 1952). The density variation
cooresponding to the transition $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I}) \rightarrow$ $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (IV) is about $23 \%$.

## Experimental

The intensity measurements were made by use of the same diffractometer and by following the same procedure described in the preceding paper. The specimen was a crystal of irregular shape, the longest dimension being $\sim 0.3 \mathrm{~mm}$. This crystal was oriented with the [001] zone axis parallel to the $\varphi$ axis of the goniostat. No absorption correction was applied because the dimensions of the crystal were such that the absorption effects were negligible. A total number of 863 independent reflections were measured; each one represents the average of at least three measurements taken on three different planes of the same crystallographic form. The symmetry of the X-ray diffraction effects for $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$ is $m 3$, in which the $h k l$ and $k h l$ reflections are different. Those reflections for which the peakheight was not at least twice as much as the background were regarded as unobserved. This criterion gave a total of 267 observed reflections and 596 unobserved ones.

## Solution of the structure

The first step in solving the structure was based on determining the position of the $\mathrm{Ca}(2)$ atoms, which are in the special positions $(x, x, x)$ of the $P a 3$ space group. It was evident from the observed structure factors that, once $\mathrm{Ca}(1)$ had been placed in the special positions $(0,0,0), \mathrm{Ca}(2)$ was very nearly at $\left(\frac{3}{8}, \frac{3}{8}, \frac{3}{8}\right)$. A three-dimensional Fourier synthesis carried out with the $F_{h k l}$ having the signs of the relative calcium contribution gave the approximate positions of the other three atoms, $\mathrm{B}, \mathrm{O}(1)$, and $\mathrm{O}(2)$. The Fourier synthesis was computed by the use of the program 'Four' written by Fritchie (1967) and modified by L. Guggenberger \& P. B. Jamieson. Since the structural arrangement obtained was reasonable from the crystal chemistry point of view, this structure was refined by the use of the least-squares program written by Prewitt (1966) with the $f$-curves for neutral calcium, oxygen and boron given by Cromer \& Waber (1965). The anomalous dispersion corrections were not applied to the $f$-curve of Ca (see the section Anomalous dispersion in the preceding paper: Marezio, Remeika \& Dernier, 1969). All observed structure factors were weighted equally. Convergence was attained after several refinement cycles of the scale factor, the extinction correction coefficient, the positional parameters and the isotropic temperature factors. The secondary extinction correction was quite small, but still appreciable. In the final refinement anisotropic temperature factors were introduced, but, as expected, there was no appreciable anisotropy. The degree of agreement between observed and calculated structure factors is shown in Table 2, where $F_{c}$ represents the calculated structure factor per unit cell. The final refinement gave a conventional $R$

Table 2. Observed and calculated structure factors for $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$

| nk ? | LFl | $\underline{F}{ }_{c}$ | hke | Lfod | LF\| | $\mathrm{n} k$ l | $\underline{\text { E }}$ | $\underline{F_{C}}$ | hk l | LFod | ${ }_{\sim}^{P}{ }_{c} \mid$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 112 | 16.3 | 15.1 | 624 | 35.2 | 86.0 | 844 | 64.5 | 65.0 | 881 | 26.6 | 24.7 |
| 200 | 21.6 | 19.4 | 642 | 26.3 | 25.3 | 853 | 14.8 | 17.1 | 1122 | 21.4 | 21.9 |
| 210 | 32.0 | 28.1 | 544 | 18.8 | 16.1 | 941 | 15.5 | 15.7 | 917 | 12.3 | 13.3 |
| 211 | 10.0 | 8.9 | 722 | 33.7 | 34.2 | 755 | 19.1 | 19.1 | 955 | 20.5 | 18.6 |
| 220 | 43.7 | 41.7 | 553 | 58.8 | 59.7 | 933 | 13.4 | 15.7 | 971 | 13.9 | 14.5 |
| 221 | 8.6 | 8.2 | 713 | 79.5 | 82.6 | 806 | 30.1 | 29.6 | 1131 | 19.8 | 20.2 |
| 311 | 224.5 | 121.0 | 731 | 67.3 | 69.4 | 860 | 26.8 | 28.0 | 882 | 23.5 | 22.6 |
| 222 | 6.9 | 8.6 | 634 | 38.3 | 36.3 | 1000 | 39.7 | 40.3 | 1044 | 19.9 | 18.2 |
| 302 | 103.5 | 102.3 | 650 | 39.2 | 37.8 | 746 | 22.0 | 22.4 | 946 | 45.4 | 42.4 |
| 312 | 21.6 | 22.1 | 615 | 54.0 | 54.7 | 764 | 10.6 | 10.6 | 776 | 32.6 | 30.6 |
| 321 | 60.4 | 58.1 | 651 | 22.8 | 22.3 | 861 | 31.9 | 32.2 | 927 | 27.7 | 27.1 |
| 400 | 72.4 | 71.8 | 723 | 27.9 | 28.7 | 942 | 47.7 | 47.9 | 972 | 47.6 | 47.1 |
| 322 | 15.0 | 13.4 | 732 | 25.2 | 25.3 | 1010 | 21.2 | 21.8 | 1035 | 31.4 | 32.2 |
| 410 | 89.2 | 86.3 | 800 | 126.5 | 131.6 | 1011 | 15.2 | 14.1 | 1053 | 21.6 | 22.1 |
| 411 | 42.6 | 41.7 | 625 | 33.1 | 34.9 | 826 | 19.7 | 19.6 | 1132 | 30.3 | 28.8 |
| 331 | 26.0 | 23.4 | 652 | 25.2 | 25.0 | 862 | 18.2 | 18.0 | 866 | 17.3 | 18.3 |
| 402 | 36.3 | 38.8 | 704 | 30.0 | 32.0 | 1002 | 27.6 | 28.5 | 1060 | 27.0 | 26.9 |
| 420 | 164.3 | 167.8 | 810 | 39.9 | 41.7 | 1020 | 22.4 | 21.0 | 883 | 17.8 | 17.8 |
| 412 | 11.3 | 9.6 | 554 | 9.7 | 9.2 | 845 | 26.9 | 27.0 | 1016 | 17.3 | 16.8 |
| 421 | 149.4 | 147.6 | 714 | 25.3 | 26.2 | 1012 | 19.9 | 20.6 | 1061 | 12.6 | 11.7 |
| 332 | 107.0 | 103.0 | 811 | 22.4 | 24.3 | 934 | 12.1 | 11.7 | 1104 | 25.9 | 25.9 |
| 422 | 44.3 | 43.2 | 733 | 18.8 | 20.2 | 773 | 33.5 | 33.8 | 857 | 12.3 | 20.6 |
| 430 | 22.5 | 21.8 | 802 | 22.2 | 23.7 | 915 | 49.2 | 50.7 | 937 | 55.5 | 54.5 |
| 413 | 20.8 | 20.8 | 820 | 30.7 | 32.3 | 666 | 35.6 | 34.9 | 973 | 13.7 | 13.4 |
| 333 | 78.5 | 76.4 | 742 | 50.6 | 51.6 | 1022 | 13.3 | 11.4 | 1133 | 32.1 | 32.4 |
| 511 | 52.6 | 54.0 | 812 | 16.9 | 17.0 | 836 | 11.2 | 10.6 | 1062 | 20.9 | 20.3 |
| 423 | 18.5 | 19.7 | 821 | 20.3 | 19.9 | 863 | 39.0 | 38.9 | 1045 | 12.5 | 11.1 |
| 432 | 38.1 | 36.5 | 635 | 77.1 | 76.7 | 1030 | 48.0 | 48.0 | 1054 | 59.6 | 57.1 |
| 502 | 26.6 | 28.1 | 822 | 33.8 | 34.6 | 756 | 31.7 | 31.9 | 1142 | 24.1 | 25.6 |
| 512 | 29.5 | 29.9 | 830 | 35.2 | 37.1 | 765 | 17.0 | 15.6 | 965 | 33.9 | 34.0 |
| 521 | 61.5 | 60.0 | 734 | 28.9 | 29.7 | 925 | 26.7 | 26.0 | 884 | 25.5 | 25.4 |
| 440 | 100.2 | 100.3 | 743 | 14.0 | 14.7 | 952 | 18.7 | 17.8 | 1200 | 14.4 | 18.0 |
| 522 | 28.1 | 28.4 | 813 | 18.1 | 20.6 | 1013 | 14.0 | 15.8 | 1210 | 40.3 | 39.1 |
| 433 | 19.7 | 20.2 | 555 | 77.8 | 77.9 | 1031 | 22.5 | 22.2 | 918 | 14.0 | 12.6 |
| 513 | 26.2 | 26.4 | 715 | 10.3 | 8.7 | 774 | 11.2 | 11.0 | 974 | 12.9 | 13.0 |
| 531 | 26.1 | 27.0 | 751 | 83.9 | 85.7 | 817 | 15.4 | 14.1 | 1134 | 15.1 | 14.3 |
| 442 | 41.2 | 39.9 | 662 | 47.5 | 48.1 | 855 | 12.0 | 11.1 | 1211 | 12.9 | 12.6 |
| 600 | 57.4 | 57.1 | 654 | 59.7 | 60.6 | 953 | 20.0 | 20.7 | 777 | 26.4 | 25.7 |
| 610 | 17.8 | 18.1 | 823 | 28.0 | 28.0 | 846 | 15.4 | 14.7 | 1125 | 18.4 | 17.7 |
| 523 | 74.6 | 73.9 | 725 | 40.5 | 41.7 | 864 | 19.7 | 20.2 | 1202 | 23.0 | 23.2 |
| 532 | 27.8 | 27.8 | 752 | 21.4 | 21.3 | 1004 | 42.5 | 41.9 | 867 | 29.9 | 29.3 |
| 611 | 51.5 | 51.4 | 840 | 61.1 | 64.2 | 1040 | 30.7 | 31.3 | 982 | 33.6 | 32.9 |
| 602 | 9.1 | 8.1 | 744 | 14.2 | 14.4 | 827 | 38.3 | 38.5 | 1070 | 34.2 | 36.2 |
| 620 | 36.0 | 37.4 | 842 | 12.8 | 12.9 | 906 | 40.2 | 42.3 | 1221 | 48.4 | 48.2 |
| 504 | 28.6 | 29.5 | 753 | 16.7 | 15.7 | 1014 | 30.6 | 31.2 | 1017 | 16.2 | 13.5 |
| 612 | 16.5 | 18.3 | 824 | 20.1 | 19.7 | 1041 | 11.4 | 9.0 | 1071 | 12.7 | 10.4 |
| 514 | 14.7 | 15.5 | 842 | 45.8 | 46.3 | 916 | 37.8 | 36.4 | 1125 | 21.6 | 21.5 |
| 541 | 7.7 | 5.7 | 706 | 58.9 | 57.5 | 961 | 21.6 | 19.7 | 1152 | 15.3 | 17.7 |
| 533 | 59.1 | 56.9 | 902 | 69.4 | 70.2 | 1033 | 48.7 | 49.1 | 1046 | 33.4 | 31.7 |
| 622 | 40.5 | 40.3 | 655 | 25.3 | 23.0 | 1042 | 27.6 | 27.4 | 885 | 12.8 | 9.8 |
| 524 | 20.4 | 22.1 | 716 | 37.1 | 37.2 | 962 | 16.2 | 15.7 | 1072 | 15.0 | 12.5 |
| 542 | 35.2 | 34.8 | 761 | 29.7 | 29.7 | 873 | 12.1 | 10.5 | 1230 | 18.7 | 18.9 |
| 630 | 59.9 | 60.1 | 912 | 37.3 | 37.4 | 775 | 22.2 | 21.1 | 938 | 24.7 | 22.7 |
| 623 | 79.9 | 81.8 | 921 | 39.8 | 40.3 | 1121 | 34.0 | 35.0 | 983 | 22.1 | 20.7 |
| 631 | 25.2 | 24.1 | 664 | 28.5 | 25.8 | 856 | 12.7 | 11.6 | 975 | 49.8 | 48.6 |
| 44 | 38.5 | 37.8 | 726 | 17.7 | 17.7 | 865 | 39.4 | 36.7 | 1135 | 31.4 | 31.1 |
| 623 | 39.3 | 39.1 | 843 | 30.7 | 31.0 | 1034 | 59.0 | 60.0 | 1106 | 14.5 | 15.3 |
| 534 | 16.7 | 16.4 | 850 | 11.4 | 7.9 | 1050 | 38.0 | 37.4 | 1232 | 16.5 | 15.6 |
| 543 | 18.2 | 18.8 | 745 | 16.2 | 15.6 | 1102 | 44.5 | 43.6 | 1037 | 21.3 | 21.0 |
| 551 | 22.1 | 20.9 | 754 | 11.4 | 9.7 | 936 | 17.9 | 16.5 | 1073 | 26.4 | 26.0 |
| 711 | 16.6 | 18.1 | 913 | 34.8 | 34.7 | 963 | 41.6 | 41.4 | 1116 | 23.8 | 23.9 |
| 640 | 11.3 | 12.1 | 931 | 30.9 | 31.9 | 1015 | 26.7 | 27.2 | 1161 | 13.0 | 11.7 |
| 614 | 64.6 | 65.7 | 825 | 15.8 | 16.1 | 1051 | 29.0 | 29.0 | 1204 | 63.0 | 62.7 |
| 641 | 24.2 | 25.4 | 852 | 13.7 | 11.9 | 1112 | 28.8 | 29.3 | 1240 | 58.8 | 57.1 |
| 702 | 97.4 | 101.4 | 736 | 53.2 | 52.9 | 1121 | 13.1 | 14.3 | 1065 | 13.6 | 10.4 |
| 33 | 48.0 | 47.1 | 923 | 27.5 | 27.0 | 880 | 51.6 | 50.9 | 1126 | 13.2 | 11.1 |
| 721 | 25.7 | 25.5 | 932 | 17.9 | 17.6 | 874 | 11.1 | 7.3 |  |  |  |

value of 0.033 and the positional and thermal parameters given in Table 3.

Table 3. Positional and thermal parameters

|  | $x$ | $y$ | $z$ | $B\left(\AA^{2}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{Ca}(1)$ | $(0)$ | $(0)$ | $(0)$ | $1 \cdot 20(3)$ |
| $\mathrm{Ca}(2)$ | $0.37305(7)$ | $(0 \cdot 37305)$ | $(0 \cdot 37305)$ | $0.57(2)$ |
| $\mathrm{O}(1)$ | $0.3336(2)$ | $0.2692(2)$ | $0.1208(3)$ | $0.59(3)$ |
| $\mathrm{O}(2)$ | $0.0906(2)$ | $0.2823(2)$ | $0.0064(3)$ | $0.64(3)$ |
| B | $0.1189(4)$ | $0.1901(4)$ | $0.3457(4)$ | $0.51(5)$ |

## Description and discussion of the structure

The results of the final refinement gave the interatomic distances and their standard deviations reported in Table 4.
The structure contains an infinite tridimensional array of $\left[\mathrm{B}_{3} \mathrm{O}_{6}\right]^{2-}$ - units as shown in Fig. 1. A projection of the unit $\left[\mathrm{B}_{3} \mathrm{O}_{6}\right]^{--}$on the (110) plane is shown in Fig. 2.

Table 4. Interatomic distances*

| $\mathrm{Ca}(1)-\mathrm{O}(1)(6)$ | $2.785(2) \AA$ |
| :--- | :--- |
| $\mathrm{Ca}(1)-\mathrm{O}(2)(6)$ | $2.671(2)$ |
| $\mathrm{Ca}(2)-\mathrm{O}(1)(3)$ | $2.483(3)$ |
| $\mathrm{Ca}(2)-\mathrm{O}(1)(3)$ | $2.598(3)$ |
| $\mathrm{Ca}(2)-\mathrm{O}(2)(3)$ | $2.385(3)$ |
| $\mathrm{Ca}(2)-\mathrm{O}(2)(3)$ | $3.142(3)$ |
| $\mathrm{B}-\mathrm{O}\left(1^{\prime}\right)$ | $1.465(4)$ |
| $\mathrm{B}-\mathrm{O}\left(1^{\prime \prime}\right)$ | $1.495(4)$ |
| $\mathrm{B}-\mathrm{O}\left(2^{\prime}\right)$ | $1.491(4)$ |
| $\mathrm{B}-\mathrm{O}\left(2^{\prime \prime}\right)$ | $1.468(4)$ |
| $\mathrm{O}\left(1^{\prime}\right)-\mathrm{O}\left(1^{\prime \prime}\right)$ | $2.407(4)$ |
| $\mathrm{O}\left(1^{\prime}\right)-\mathrm{O}\left(2^{\prime}\right)$ | $2.94(4)$ |
| $\mathrm{O}\left(1^{\prime}\right)-\mathrm{O}\left(2^{\prime \prime}\right)$ | $2.422(3)$ |
| $\mathrm{O}\left(1^{\prime \prime}\right)-\mathrm{O}\left(2^{\prime}\right)$ | $2.403(3)$ |
| $\mathrm{O}\left(1^{\prime \prime}\right)-\mathrm{O}\left(2^{\prime \prime}\right)$ | $2.427(3)$ |
| $\mathrm{O}\left(2^{\prime}\right)-\mathrm{O}\left(2^{\prime \prime}\right)$ | $2.441(4)$ |

* These interatomic distances and their standard deviations were obtained with the Busing, Martin \& Levy program ORFEE (1964). The standard deviations reflect the use of unit weights in the least-squares refinement of the structure.

It consists of a ring of three $\mathrm{BO}_{4}$ tetrahedra having two of their vertices in common. The three oxygens which are shared among the three tetrahedra which form the ring are $\mathrm{O}(1)$, whereas the six oxygens which are shared with other units are $O(2)$. One unit shares the six $\mathrm{O}(2)$ atoms with six different units. This array of boron-tetrahedra forms large empty cages in which the calcium atoms are accomodated. The mean B-O distance is $1-480 \AA$ with individual distances varying from 1.465 to $1 \cdot 495 \AA$. There are two types of calcium atom in this structure. $\mathrm{Ca}(1)$ is at the origin and is surrounded by a 12 -oxygen polyhedron which is shown schematically in Fig.3. In the polyhedron there are two sets of six $\mathrm{Ca}-\mathrm{O}$ distances, $\mathrm{Ca}(1)-\mathrm{O}(1)=2.785 \AA$ and $\mathrm{Ca}(1)-\mathrm{O}(2)=2.671 \AA$. As far as we know this is the first observation of coordination twelve for calcium in oxide compounds. $\mathrm{Ca}(2)$ is on a threefold axis and is surrounded by three sets of three oxygen atoms at $2.385 \AA, 2.483 \AA$ and $2.598 \AA$. In addition to these first nearest oxygen atoms there is one set of three oxygen atoms at $3 \cdot 142 \AA$. These twelve oxygen atoms form a very irregular polyhedron. When there is such a large variation among the distances in the same polyhedron it is very difficult to determine the coordination number of the cation, the true coordination being between 9 and 12. In fact, the average of the first nine $\mathrm{Ca}-\mathrm{O}$ distances, $2.489 \AA$, is much shorter than the value of $2.57 \AA$ given by International Tables for $X$-ray Crystallography (1962) as the average $\mathrm{Ca}-\mathrm{O}$ distance for 9 -coordinated calcium. Furthermore, the average of the first twelve $\mathrm{Ca}-\mathrm{O}$ distances, $2 \cdot 652 \AA$, is much shorter than the average of the twelve distances $\mathrm{Ca}(1)-\mathrm{O}$, $2.728 \AA$. The coordination number of the oxygen atoms is five; each one is surrounded by one $\mathrm{Ca}(1)$, two $\mathrm{Ca}(2)$, and two boron atoms.

If one assigns a bond strength of 0.75 to each B-O bond and 0.17 to each $\mathrm{Ca}-\mathrm{O}$ bond, the bond strength of both $\mathrm{O}(1)$ and $\mathrm{O}(2)$ is $2 \cdot 0$, indicating that in this structure the distortion of the boron and calcium polyhedra must be ascribed to next nearest neighbor interactions.

## Polymorphism of $\mathrm{CaB}_{2} \mathrm{O}_{4}$

Data for the polymorphism of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ are summarized in Table 5. Calcium metaborate can crystallize with four different structures, three orthorhombic and one cubic. In the phase stable at normal pressure all boron atoms are triangularly coordinated, while the calcium atoms are each surrounded by an 8 -oxygen polyhedron (Marezio, Plettinger \& Zachariasen, 1963b).

In the structure of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (II) $50 \%$ of the boron atoms are triangularly coordinated and $50 \%$ tetrahedrally coordinated. The calcium atoms have the same coordination number 8 as in $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})$ (Zachariasen, 1968). Therefore, in the transition (I) $\rightarrow$ (II) the only cations that increase their coordination are $\frac{1}{2}$ of the boron atoms. The density variation corresponding to this transition is $6.5 \%$. The high pressure experiments made in order to prepare $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{II})$ seem to indicate
that the pressure range of stability of this phase is very narrow, around $12-15 \mathrm{kbar}$. We have not been able to obtain pure $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{II})$, but always together with the starting material, namely $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})$.
$\mathrm{CaB}_{2} \mathrm{O}_{4}$ (III) can be synthesized at $900^{\circ} \mathrm{C}$ under a pressure of about $15-25 \mathrm{kbar}$. In this phase $\frac{1}{3}$ of the boron atoms are triangularly coordinated and $\frac{2}{3}$ tetrahedrally coordinated, while $\frac{2}{3}$ of the calcium atoms are


Fig.1. The structure of $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$ viewed along the $c$ axis. The boron atoms at the centers of the tetrahedra are omitted for clarity. The filled and open circles represent $\mathrm{Ca}(1)$ and $\mathrm{Ca}(2)$ respectively. Note that a left-handed system of axes has been used.


Fig. 2. A projection on the (110) plane of the three-tetrahedra unit $\left[\mathrm{B}_{3} \mathrm{O}_{6}\right]^{-3}$. As can be seen from Fig. 1, these units are linked together to form a three-dimensional network.

8 -coordinated and $\frac{1}{3} 10$-coordinated (Marezio, Remeika, \& Dernier, 1969). In the transition (I) $\rightarrow$ (III) $\frac{2}{3}$ of the boron and $\frac{1}{3}$ of the calcium atoms increase


Fig.3. The oxygen-polyhedron around $\mathrm{Ca}(1)$. If one considers the calcium atom as part of the array, this polyhedron forms a cubic close-packed array.
their coordination, while in the transition (II) $\rightarrow$ (III) $\frac{1}{6}$ of the boron and $\frac{1}{3}$ of the calcium atoms increase their coordination. The density variations corresponding to these two transitions are $12 \cdot 2 \%$ and $5 \cdot 6 \%$, respectively.

The structure of $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{III})$ contains $\left[\mathrm{B}_{6} \mathrm{O}_{12}\right]^{2-}$ units consisting of two triangular and four tetrahedral boron oxygen groups (see Fig. 2 of the preceding paper: Marezio etal. 1969). In this unit there is a ring of three tetrahedra which have two of their four corners in common. These rings are maintained in the structure of $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (IV) (see Figs. 1 and 2). In the transition (III) $\rightarrow$ (IV) $\frac{1}{3}$ of the boron atoms increase their coordination from 3 to 4 , whereas $\frac{2}{3}$ of the calcium atoms increase their coordination to $9-12$ and $\frac{1}{3}$ to 12 . The density variation corresponding to this transition is $11 \cdot 5 \%$.

## Polymorphism in borates

Many classifications have been proposed for borates. The latest to appear is the one by Bokii \& Kravchenko (1966). It is not our intention to propose new criteria for classifying borates, but we would like to point out that an interesting feature arises if one classifies the borates according to the coordination of the boron atoms. In Table 6 several anhydrous borates are classified according to this criterion. It should be noted

Table. 5. Polymorphism of $\mathrm{CaB}_{2} \mathrm{O}_{4}$

| $\mathrm{CaB}_{2} \mathrm{O}_{4}$ | $\begin{gathered} \text { Approximate } \\ \text { range of } \\ \text { stability at } 900^{\circ} \mathrm{C} \end{gathered}$ | Density $\left({\mathrm{g} . \mathrm{cm}^{-3}}\right)$ | Symmetry | Lattice parameters ( $\AA$ ) | No. of molecules per unit cell | \% $B \triangle$ | \% B $\triangle$ | Ca (C.N.) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (I) | $0-12 \mathrm{kbar}$. | 2.702 | Orthorhombic | $\begin{aligned} & a=6.214 \\ & b=11.604 \end{aligned}$ | 4 | 100 | 0 | 8 |
| (II) | 12-15 kbar. | 2.885 | Orthorhombic | $\begin{aligned} & c=4.285 \\ & a=8.369 \\ & b=13.816 \end{aligned}$ | 8 | 50 | 50 | 8 |
| (III) | 15-25 kbar. | $3 \cdot 052$ | Orthorhombic | $\begin{aligned} & c=5.007 \\ & a=11.380 \\ & b=6.382 \end{aligned}$ | 12 | 33 | 67 | $\begin{array}{ll} 67 \% & 8 \\ 33 \% & 10 \end{array}$ |
| (IV) | 25-40 kbar. | $3 \cdot 426$ | Cubic | $\begin{aligned} & c=11.304 \\ & a=9.008 \end{aligned}$ | 12 | 0 | 100 | $\begin{aligned} & 67 \% \quad 9-12 \\ & 33 \% 12 \end{aligned}$ |

Table 6. Classification of some anhydrous borates accoding to the boron atom coordination

| All $\triangle$ | $4 \triangle: 1 \triangle$ | $3 \triangle: 1 \triangle$ | $2 \mathrm{\Delta}$ : $1 \triangle$ | $1 \triangle: 1 \triangle$ | $1 \triangle: 2 \triangle$ | All $\triangle$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{NaBO}_{2}{ }^{(1)}$ | $\mathrm{KB}_{5} \mathrm{O}_{8}{ }^{(8)}$ | $\mathrm{Ag}_{2} \mathrm{~B}_{8} \mathrm{O}_{13}(10)$ | $\mathrm{HBO}_{2}(\mathrm{II})^{(11)}$ | $\mathrm{CdB}_{4} \mathrm{O}_{7}(12)$ | $\mathrm{CaB}_{2} \mathrm{O}_{4}$ (III)(15) | $\mathrm{SrB}_{2} \mathrm{O}_{4}(\mathrm{IV})^{(16)}$ |
| $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{I})^{(2)}$ | $\mathrm{RbB}_{5} \mathrm{O}_{8}{ }^{(9)}$ |  |  | $\mathrm{Li}_{2} \mathrm{~B}_{4} \mathrm{O}_{7}{ }^{(13)}$ | $\mathrm{SrB}_{2} \mathrm{O}_{4}(\mathrm{III})^{(16)}$ | $\mathrm{B}_{2} \mathrm{O}_{3}(\mathrm{II})^{(17)}$ |
| $\mathrm{HBO}_{2}(\mathrm{I})^{(3)}$ |  |  |  | $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{II})^{(14)}$ |  | $\mathrm{HBO}_{2}(\mathrm{IIII})^{(18)}$ |
| $\mathrm{LiBO}_{2}(\mathrm{I})^{(4)}$ |  |  |  |  |  | $\mathrm{SrB}_{4} \mathrm{O}_{7}(19)$ |
| $\mathrm{SrB}_{2} \mathrm{O}(\mathrm{I})^{(5)}$ |  |  |  |  |  | $\mathrm{LiBO}_{2}(\mathrm{III})^{(20)}$ |
| $\mathrm{BaB}_{2} \mathrm{O}_{4}{ }^{(6)}$ |  |  |  |  |  | $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})^{(21)}$ |

(1) Marezio, Plettinger \& Zachariasen (1963a)
${ }^{(2)}$ Marezio, Plettinger \& Zachariasen (1963b)
(3) Peters \& Milberg (1964)
(4) Zachariasen (1964)
(5) Block, Perloff \& Weir (1964)
(6) Mighell, Perloff \& Block (1966)
${ }^{(7)}$ Gurr, Montgomery, Knutson \& Gorres (1967)
(8) Krogh-Moe (1965b)
(9) Krogh-Moe (1959)
(10) Krogh-Moe (1965a)
(11) Zachariasen (1963a)
(12) Ihara \& Krogh-Moe (1966)
(13) Krogh-Moe (1968)
(14) Zachariasen (1968)
${ }^{(15)}$ Marezio, Remeika \& Dernier (1969)
(16) Dernier (1968)
(17) Prewitt \& Shannon (1968)
(18) Zachariasen (1963b)
(19) Krogh-Moe (1964)
(20) Marezio \& Remeika (1966)
(21) This paper
that all compounds in which the boron atoms have coordination number 4 have been reported to be high pressure phases with the exception of $\mathrm{Sr}_{4} \mathrm{O}_{7}$. KroghMoe (1964) has reported the synthesis and the structure of this compound. Crystals of $\mathrm{SrB}_{4} \mathrm{O}_{7}$ can be prepared from a melt with a slight excess of $\mathrm{B}_{2} \mathrm{O}_{3}$ at $900^{\circ} \mathrm{C}$.
One of us is studying the behavior of $\mathrm{SrB}_{2} \mathrm{O}_{4}$ under pressure (Dernier, 1969). Preliminary results seem to indicate that $\mathrm{SrB}_{2} \mathrm{O}_{4}$ behaves under pressure very much in the same way as $\mathrm{CaB}_{2} \mathrm{O}_{4}$. One interesting difference is that $\mathrm{SrB}_{2} \mathrm{O}_{4}(\mathrm{IV})$, an isomorph of $\mathrm{CaB}_{2} \mathrm{O}_{4}(\mathrm{IV})$, decomposes at about 40 kbar and $900^{\circ} \mathrm{C}$. One of the products of decomposition is $\mathrm{SrB}_{4} \mathrm{O}_{7}$, as identified from an X-ray powder photograph of the quenched material. The crystals of $\mathrm{SrB}_{4} \mathrm{O}_{7}$ have been synthesized at normal pressure, but the structure (Krogh-Moe, 1964) has all the features of a high pressure structure. The cations have high coordination, all the boron atoms are tetrahedrally coordinated and the strontium atoms have 16 nearest neighbors. Although they are not all first nearest neighbors, it is a very high coordination for strontium. Furthermore, some oxygen atoms are bonded to three boron atoms. This feature has been found in the mineral tunellite (Clark, 1963), and recently in the high pressure phase $\mathrm{B}_{2} \mathrm{O}_{3}$ (II) (Prewitt \& Shannon, 1968). The calculated density,. $4.02 \mathrm{gr.cm}^{-3}$, also seems to indicate that the structure of $\mathrm{SrB}_{4} \mathrm{O}_{7}$ is a compact one.
Table 6 seems to indicate that many new phases can be synthesized under pressure. New phases should exist for all those compounds in which the boron atoms are not all tetrahedrally coordinated. It is difficult toforesee how many phases exist for each compound, but by analogy to $\mathrm{CaB}_{2} \mathrm{O}_{4}$ and $\mathrm{HBO}_{2}$ we would expect that more than one high pressure phase should exist for the metaborates, $\mathrm{BaB}_{2} \mathrm{O}_{4}, \mathrm{NaBO}_{2}$ and $\mathrm{KBO}_{2}$ and at least one for the polyborates. For instance, at high pressure $\mathrm{CdB}_{4} \mathrm{O}_{7}$ should be isostructural with $\mathrm{SrB}_{4} \mathrm{O}_{7}$. We also believe that more high pressure phases should exist for $\mathrm{B}_{2} \mathrm{O}_{3}$. At present we are investigating the behavior of $\mathrm{BaB}_{2} \mathrm{O}_{4}$ under pressure.

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